The anterior cruciate ligament (ACL) is an essential stabilizing soft tissue of a knee joint that is often the cause of traumatic injuries. Approximately 100,000 to 200,000 ACL ruptures occur each year in the United States. The high rate of ACL injury explains the dramatic increase in the number of surgical reconstruction (ACL-R) procedures performed to avoid any secondary damage, thereby restoring the standard and high level of physical activity. Although ACL-R provides short-term success in restoring stability and functional improvement, the procedure does not offer protection...
against early-onset joint degeneration and the development of osteoarthritis (OA) in the population with an ACL-reconstructed knee.6 The earlier observation was confirmed by the high level of dissatisfaction, which reached 40%, and the high percentage (82 to 89%) of the degenerative radiographic changes observed within the treated population.5–8 In addition to the associated defect due to initial trauma, in part, the initiation of OA may be attributed to the abnormal loading conditions of the reconstructed joint. The abnormal loading conditions may be mediated by surgical parameters such as single or double-bundle reconstruction, attachment sites, angle of fixation, graft pretension and tunnel orientations, or the patients’ specific parameters such as postsurgical muscle activation patterns and joint geometry.9,10 Despite the high correlation between the ACL-R treatment and posttraumatic knee OA, the exact etiology of this degenerative disease is not fully understood.11

Evidence indicates that the natural kinematics and kinetics of a knee joint are not restored following ACL-R with either a patellar tendon or hamstring tendon graft.12–17 Furthermore, the loading conditions translated by contact behavior alterations, specifically on the articular cartilage, may impose a mechanical insult on areas that are not commonly loaded.18 The new load distribution may lead to a more rapid degradation of the underlying tissue.8,19 Surprisingly, the degree to which ACL-R affects the joint contact mechanics is not apparent yet. Indeed, except few published studies, the majority have not provided an accurate quantitative assessment of the essential variables of interest such as compartmental and total contact forces and areas as well as the distribution of stresses/strains.20–25 Both experimental and computational studies focused on the effect of a limited number of surgical parameters such as the angle of flexion at the time of the graft fixation, the graft pretension, and the attachment sites on the joint’s biomechanics under well-known clinical tests like Lachman and pivot tests.14,19,22,24,26–32 The results reported in those studies have been characterized by significant discrepancies, due to the high variability of the surgical procedures and complexity of the interaction of the surgical parameters. However, the relative contributions of the surgical variables to the knee biomechanical response remain unclear; specifically, the tibiofemoral articular cartilages’ contact response following an ACL-R.

In the current investigation, we adopted a systematic engineering approach to study the sensitivity of joint contact behavior to the surgical simulations of the bone-patellar-tendon-bone (BPTB) ACL-R procedure. The use of the sensitivity analysis framework is advantageous due to the multifactorial nature of the problem. A calibrated and validated healthy model and an ACL-R model13–35 were used to identify the effect of the femoral tunnel’s vertical and horizontal locations, femoral sagittal and coronal orientations, fixation angle and graft pretension on cartilage contact patterns, as estimated during isolated tasks (axial compression). Due to their correlation with cartilage degeneration and OA initiation,16 the compartmental contact force and area, contact center location, and average and maximum contact stresses were considered as the output variables of interest.

Methods

Finite Elements Models and Simulations of the ACL-R Surgery:

A previously developed computational model of the knee joint comprising all relevant soft tissues was employed in the present study.36–37 The knee model includes three bony structures (tibia, femur, and patella) associated with the articular cartilage layers, menisci and the eight principal ligaments, anterior/posterior cruciate ligaments (ACL/PCL), medial/lateral collateral ligaments (LCL/MCL), medial/lateral patellofemoral ligaments (MPFL/LPFL), and patellar tendon and quadriceps ligament (PT/QL). The meshes of tibial, patellar and femoral articular cartilages as well as menisci were extensively refined. Furthermore, local elements’ system axes were created to allow accurate incorporation of collagen networks and solid matrix depth-dependent properties variation. The collagen fibrils were oriented horizontally parallel to the medial/lateral and anterior/posterior directions in the cartilage’s superficial zone. In the transitional zone, the random fibrils (i.e., no dominant orientations) followed a gradual curvature, beginning with parallel orientations and turning perpendicular to the surface close to the deep zone. In the deep zone, vertical fibrils were primarily oriented normal to the subchondral junction. In menisci, element properties were oriented in the circumferential and radial directions, based on the local coordinate system’s axes orientations. For more details of the model’s development process, please see the Supplementary Materials (available online only) and our prior published studies.36–40

The aforementioned knee model has been updated with additional features and associated changes to develop the parametric FE model of biomechanical experiments which depict the ACL-R surgery. Accordingly, the model included tibial and femoral tunnels of 9 mm diameter with the exact geometry of BPTB graft, which was incorporated by separating the geometry of the graft from that of PT (►Fig. 1). Thereafter, a population of the models was created with respect to six intraoperative variables, two-quadrant coordinates of femoral tunnel placement, sagittal and coronal angles of the femoral tunnel, the graft tension, and the joint angle at which the BPTB graft is tensioned and fixed to the femoral tunnel (fixation angle) (►Supplementary Fig. S1). For more details, please see Supplementary Materials (available online only). A number of steps were adopted sequentially to conduct the surgical simulation; first, the proximal bone plug was placed inside the femoral tunnel, aligned with the tunnel axis. Second, the distal bone plug was placed and fixed in the tibial tunnel, with the proximal bone plug constraint to rotate and slide about the femoral tunnel axis. In the third simulation step, the tibia was flexed to a given fixation angle. Over the next step, the proximal bone plug was pulled along the femoral tunnel axis, using a given pretensioning force, keeping the tibia free in all degrees of freedom. Finally, the joint was fully extended, and the surgical simulation was completed (►Supplementary Fig. S5 in the Supplementary Materials).
Materials Section [available online only]). A subsequent simulation step was also introduced, where the knee joint was axially loaded under full extension by 1000 N to predict joint contact parameters. The femur was fixed under the applied compression force, while the tibia was left free, except the flexion-extension degree of freedom. All the boundary conditions were applied at the reference points (RP) of the femoral and tibial bones (► Fig. 1A). The observed similarity with the joint’s load under single-leg standing activity,41,42 the earlier validation and verification of the healthy model, and the achieved numerical convergence were the main motives behind the choice of 1000 N axial compression load. Detailed descriptions of the statistical calibration and validation of healthy and ACL-R models have been discussed in the ► Supplementary Materials (available online only) and our prior investigations.33,34,43

Material Properties:
For the ligaments, a transversely isotropic hyperelastic material model assumed to be nearly incompressible and driven by an uncoupled representation of the strain energy function, as defined by Limbert and Middleton, was employed. In this framework, the fibers were assumed to be extensible and uniformly distributed in the ground substance and perfectly bonded to the matrix, while the matrix was assumed to be isotropic and hyperelastic. The menisci were considered as transversely isotropic, linearly elastic, and homogeneous material.35 Multiplicative decomposition of the deformation gradient into elastic and plastic parts is introduced in the present work to create the fiber-reinforced composite model of cartilage. Therefore, a hierarchical hyperelastoplastic composite material starting from tropocollagen molecules level (300 nm) to continuum macrolevel (100 µm) has been considered in the proposed model. Fundamentally, for soft tissues, the plastic flow is associated only with the uniaxial deformation of the collagen fibril.45,46 Furthermore, the yield strength ($g_0$) of the fibril is a function of the cross-link density ($\beta$) between the tropocollagen molecules, defined herein by the density function $g_0$ ($\beta$). A coarse-graining procedure was employed to link the nanoscale collagen features and the tissue-level materials properties, using the cross-link density function as a building block. Neo-Hookean generalized strain energy was used to model the micro-fibrils, fibrils, and tissue behavior by considering the rule of mixtures. A 0.001 g/mm$^3$ density was assigned to all soft tissues,47 while the rigid bony segments were assigned a density of 0.002 g/mm$^3$.3,48 Details on the assigned materials’ properties have been given in the ► Supplementary Materials (available online only) as well as our prior investigations.35,37,38,40

Sampling and Surrogate Modeling:
The 6D space of surgical parameters was sampled using Maximin Latin hypercube sampling (LHS) algorithm. The sampling technique was considered to facilitate the addition of new training points to the formerly sampled space, in order to improve the precision of surrogate models. Reasonable bounds for the surgical parameters relative to data reported in a large body of the literature were employed. The parameter space was mapped using a radial basis
function (RBF) to approximate the simulation response (contact parameters). The minimum error of the RBF approximation was achieved with 48 training points.

**Probabilistic Sensitivity Analysis**

The surrogate-based approach was employed to circumvent several executions of the computationally expensive ACL-R FE models during the probabilistic sensitivity analysis. Global sensitivity analysis based on variance decomposition, as described by Saltelli et al., was employed to investigate the contributions of surgical parameters to the uncertainty in the response of the ACL-R joint. Hence, the contributions of a set of input parameters to the uncertainty in response output can be quantified by ranking the parameters, based on the output variance when one of the parameters is fixed to its true value. The expectation of all possible values of the input parameters was considered here to circumvent the surgical parameters’ unknown true values (input parameters). Based on the above description, equation (1) has been used to determine the sensitivity indices which is given by:

\[
S_i = \frac{V\left(E\left(Y|X_i\right)\right)}{V\left(Y\right)} \quad (2)
\]

\[
S_{ij} = \frac{V\left(E\left(Y|X_i,X_j\right)\right) - V\left(E\left(Y|X_i\right)\right)}{V\left(Y\right)} \quad (3)
\]

where \( S_i \) and \( S_{ij} \) are the first and the subsequent orders of sensitivities. These indices were calculated based on the following equations:

The results show that lower graft fixation angle and tensioning force were the most considerable parameters controlling the variance of the joint’s total contact force (nearly 70%), among which 37% of the variance was due to the combined action of both parameters (fixation angle and tensioning force), 18% originated by the fixation angle, and the rest of 15% by the tensioning force. Tunnel placement was the second most crucial factor that accounted for 23% of the variance. The combined effect of the graft fixation angle and vertical tunnel location is primarily responsible for the variance (i.e., nearly 78%) in the contact area, whereas the fixation angle alone is responsible for 43% variance. However, the variance in the contact center shift was explained by the tunnel placement (46%) and followed by the graft fixation angle (34%). Finally, it is found that both combined

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and individual changes in the graft tensioning force and fixation angle mainly control the sensitivity of the computed maximum contact stress (Fig. 10).

**Discussion**

With reference to our prior computational studies on the effect of the critical surgical design parameters on the intra- and postoperative variables for a BPTB ACL-R surgery, the current work aimed to investigate the effect of the surgical parameters on the articular contact behavior during axial knee compression. The targeted outcomes are the joint's total and compartmental forces and areas, the contact center location, and the average and maximum contact stresses. Our analyses indicated that the variation in the tunnel's vertical location (anterior-posterior), the graft pretension, and the
The contact force supported by the lateral compartment was found to increase significantly by almost 130 N to 215 N when the orientations of the femoral tunnel and the graft tensioning force were set nearly to the lower and upper bounds of the considered range of variations of these parameters, that is, 19° on the sagittal plane, 43° on the coronal plane, and 120 N for the maximum graft tensioning force, respectively (►Fig. 2A). This augmentation may be attributed to the predicted and measured increase of the normal force at the tunnel-graft interface that was associated with lower tunnel angles and higher pretensioning graft force.\(^{31,34,43,51}\)

The orientation of this normal force seems to be responsible for the lateral increase in the knee compartmental load. However, the observed augmentation of the lateral compartmental load was associated with a slight decrease in the medial force ranging from 40 N to 80 N. The medial force was substantially decreased by nearly 34% when the surgery adopted a low graft pretensioning force (23 N), a low fixation angle (12°), and a low sagittal orientation of the femoral tunnel (28°), which were all associated with an anterior and inferior location of the tunnel (►Fig. 2B). It is worth mentioning that this design was characterized by a loose knee during the Lachman test,\(^{43}\) an observation that was well corroborated by in vitro studies and mostly related to a low graft pretensioning force.\(^{29,52-55}\) Only one model had higher compartmental loads of nearly 100 N on both the medial and lateral sides. This model was characterized by a high fixation angle of 38° and extreme superior-posterior tunnel locations (horizontal and vertical locations 22% and 28%, respectively). These findings suggest that the graft pretensioning force may not be the only factor contributing to the dramatic increase in the contact loading. The superior-posterior location of graft insertion and the high angle of fixation may also
contribute to the aberrant contact force observed after the surgery. These earlier observations of the surgical design parameters’ effect on the compartmental load distribution may help in designing optimal surgical procedures. These procedures may improve the kinematics and the kinetics of the unstable ACL-deficient knee with varus malalignment and medial compartment knee OA. In other words, the double conservative corrections (ACL-R and knee osteotomy) may be replaced by one procedure (ACL-R).

Our results also indicated that a combination of specific surgical parameters might lead to a reconstructed total contact force of 1045 N, which is consistent with those computed for the intact joint when subjected to the same axial compression loading. More specifically, 8 out of 48 models exhibited a total contact force within 30 N (±30 N) of that computed for the intact joint. However, 3 of these 8 models were characterized by an aberrant distribution of the compartmental load that differed more than 180 N between the tibial plateaus in the extreme case. These results suggest that the knee joint’s total contact force should be carefully considered if it is used to evaluate the ability of ACL-R surgery, in order to restore the tibiofemoral contact behavior.

The compartmental and total forces of only one model fell within the range of the reported value of the intact model. For this particular model, the graft was fixed at 19° with a pretensioning force of 85 N, the femoral tunnel locations were 27% vertically and 13% horizontally, and the orientations were 48° coronal and 36° sagittal. This design successfully restored joint stability during the Lachman test but with a very high-stress concentration in the femoral graft-tunnel interface. It is worth noting that the models with the lowest contact force values (898 N and 912 N) have been characterized mainly by a noticeable difference in their applied pretensioning force (71 N and 23 N) and vertical location (67% and 26%). Thus, a high graft pretensioning force associated with an anterior tunnel position (high vertical location) led to a minimum level of contact force. This observation is consistent with the findings reported in earlier published studies, indicating a loose reaction of the operated joint with low graft pretension or more anterior insertion of the tunnel.

Most of the designs used in this investigation showed an apparent decrease in the contact area of the total and individual tibial plateaus (Fig. 3). The decrease in the contact area in some of the models was as high as 50%, particularly in the medial plateau. Our contact area data was
comparable to the results reported in a previous study using cadaveric knees. An apparent decrease in the contact area is shown for a single-bundle ACL-R in comparison to both a double-bundle ACL-R case and an intact case. Unfortunately, it is essential to note that most of the models that have successfully restored the contact force fail to restore the contact area. For example, a reduction of almost 250 mm² of the total contact area was computed with the design that most closely restored the knee to the intact contact force of 1045 N. However, only two models were nearly able to restore both the contact force and contact area properly. These models were characterized, respectively, by fixation angles of 14° and 11°, vertical locations of 49% and 33%, horizontal locations of 23% and 8%, coronal orientations of 46° and 56°, sagittal orientations of 27° and 48°, and pretensioning forces of 73 N and 36 N. Yet, these models increased the joint’s laxity by approximately 50%, which was considered to be a significant limitation. Furthermore, an apparent augmentation of the average and maximum contact stress was computed with most of the designs considered in this study. The stress concentration was localized more on the medial compartment than the lateral compartment. This result may be explained by the observed discrepancy between the force and the contact area, especially the aberrant decrease in the contact area of the medial compartment. Also, the common factors between all the models, which were characterized by 50% augmentation of the maximum contact stress, were the high values of the angle at which the graft was fixed and the graft pretension. It is important to note that, for some of the designs, even those with a lower contact force than the intact one, we computed approximately 30% higher contact stress, which can be primarily explained by the alteration of the contact area. These earlier results may shed light on the association

### Table 1 Surgical design parameters for the selected samples shown in Fig. 6

<table>
<thead>
<tr>
<th>Sample number</th>
<th>Sagittal angle (°)</th>
<th>Coronal angle (°)</th>
<th>Horizontal quadrant coordinate (h%)</th>
<th>Vertical quadrant coordinate (v%)</th>
<th>Fixation angle (°)</th>
<th>Tensioning force (N)</th>
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</thead>
<tbody>
<tr>
<td>1</td>
<td>28.23</td>
<td>74.67</td>
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<td>6.25</td>
<td>92.99</td>
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<tr>
<td>11</td>
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<td>48.75</td>
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<td>31</td>
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<td>68.28</td>
<td>46.05</td>
<td>61.12</td>
<td>25.08</td>
<td>39.79</td>
</tr>
</tbody>
</table>

Fig. 6 Knee contact pressure distribution at full extension under 1000 N axial compression of four sample models selected at random from the 48 models constructed for this paper. Table 1 provides the corresponding surgical design parameters for the selected samples.
between knee cartilage degeneration and the decrease in the joint loading observed after ACL deficiency or ACL-R. \(^{17,22,64}\)

In this study, our sensitivity analysis indicated that changes in the cross-terms (second orders indices) are more dominant than those in the first-order indices (\(\text{Figs. 7–10}\)). This observation emphasizes the importance of the interconnection between the surgical parameters that were considered during this investigation. \(^{50}\) For example, the combined action of the graft pretension, vertical tunnel location, and sagittal tunnel orientation accounted for a significant portion of the variance (62%) in the lateral contact force. While the medial contact force was most sensitive to the tunnel location by a variability of 56%, it was mainly dominated by the combined variation in the horizontal and vertical sites (36%), followed by the vertical site only (20%). These observations suggest that femoral tunnel location and graft pretension have the most significant effect on the compartmental load distributions that could lead to an aberrant load on the medial side or lateral side; hence, leading to the potential of cartilage degeneration. \(^{25,29}\) However, with earlier surgical parameters affecting the compartmental load distribution, the fixation angle was considered to be the additional principal factor contributing to the total contact force variability (only the sensitivity of the total contact force was presented here). This result is consistent with the findings reported by Mae et al. \(^{30}\) who observed a stiffer postoperative joint with the augmentation of the angle of fixation. The combined action of tunnel location and fixation angle contributed to the variability of the area and the center of the contact by 84% and 91%, respectively.
The sensitivity of the articular cartilage’s maximum contact stress, which is considered to be an essential predictor of cartilage damage initiation and propagation, was mostly affected by the graft pretension and fixation angle (86% of variability). This variability was dominated by the graft pretension (31%), followed by the fixation angle (28%), and then by their combined action (27%). It is interesting to note that the fixation angle, the tunnel locations, and graft pretension were the most common surgical parameters affecting the tibiofemoral contact behavior. However, this behavior was almost insensitive to the tunnel’s coronal and sagittal orientations, except for the case of the lateral compartment load. These findings highlight the complexity associated with the restoration of knee joint contact behavior after ACL-R surgery. Additionally, such observation may explain the well-documented evidence of posttraumatic cartilage degradation.\(^9,10\)

The computational framework and the outcomes of the current work are circumscribed by a few limitations. First, only one joint loading scenario was simulated during the investigation. Second, the capsular ligament around the knee joint was not considered in the knee model. Third, hypereelastic behavior was used as a proxy of the soft tissues’ biphasic behavior in the model. However, this proxy has been well-documented as an approved tool to accurately capture the transient response of soft tissue.\(^5,5\) Fourth, the ACL-R models do not consider structural changes (tunnel expansion) or changes in the contact properties, either in the interface of the tunnel-graft area or within the tibiofemoral joint. While graft remodeling and cycling loading can change the initial stress within the graft over time,\(^6,6\) in the present study, the wide range of initial pretension values (20 N to 120 N) included possible graft tensions at different time intervals postoperatively; hence, the findings gleaned from the current sensitivity analysis can be generalized to postsurgical states. Moreover, the current model did not account for the potential posterior tibial sag attributed to the patient’s intraoperative supine posture, a posterior displacement that may affect the joint’s kinematics after the surgery.\(^5,5\) Finally, this study did not consider muscles. However, incorporating these components may improve the accuracy of the simulation of the daily activities of the knee joint and rehabilitation treatments.\(^5,5\)

In conclusion, the current investigation used a systematic engineering approach to assess the relative influence of the surgical design parameters associated with ACL-R surgery on postoperative knee joint contact mechanics. To the best of our knowledge, this is the first model ever published in which the surgery outcomes are computed as a function of the simultaneous interaction of a high number of surgical factors (six factors). The results provide an evaluation of how the surgical parameters can affect a knee joint’s contact behavior after an ACL-R. This evaluation shows the clear differences in contact behavior during axial compression in ACL-R knees in comparison to a normal knee. The contact alterations may relate to the high incidence of knee OA observed in this population over time. In the context of the design of prospective studies, our findings evaluate the ACL-R surgery variables to restore the articular contact parameters by highlighting the importance of the tunnel’s placement, graft pretension, and flexion angle at the time of fixation.

Authors’ Contributions
All authors have read and approved this submission. The first author carried out analyses. All participated in the definition, design, and development of the work. Finally, the manuscript was written by all authors.

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Conflict of Interest
None declared.

References
Effect of Surgical Design Variations on the Knee Contact Behavior

Adouni et al.


42 Noyes SB-WDF. ACL Injury Rehabilitation: Everything You Need to Know to Restore Knee Function and Return to Activity. Cincinnati, United States: Noyes Knee Institute; 2012


48 Hoffer MM. A primer of orthopaedic biomechanics. JAMA 1983;249(17):2397


58 Sanford BA, Williams JL, Zucker-Levin AR, Mihalko WM. Tibiofemoral joint forces during the stance phase of gait after ACL reconstruction. Open J Biophys 2013;3(04):8
64 Konrath JM, Saxby DJ, Killen BA, et al. Muscle contributions to medial tibiofemoral compartment contact loading following ACL reconstruction using semitendinosus and gracilis tendon grafts. PloS One 2017;12(04):e0176016